

# Probabilistic Weather Forecasting via Bayesian Model Averaging and EMOS

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Joint work with Tilmann Gneiting

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  - **wind speed soon to be added**

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  - For Canada (Wilson et al 2007)
  - For Europe (KNMI/DWD experiments)

# UW Ensemble Bayesian Model Averaging

[User's Guide](#)

Param:

Valid for 24 hours ending at:



**Wed May 27, 2009 5 PM**



[Jump to new date](#)



Toggle Contour Lines OFF

Plot Size:  Big  Medium  Small

Units:  Celsius  Fahrenheit

Grid Forecast:

Deterministic

Upper bound of interval

Lower bound of interval

Half-width of interval

Prob. param exceeds threshold

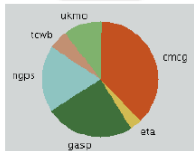
Greater than  Less than

Probability Distribution:

Latitude:

Longitude:

[Retrieve Data](#)



[BMA Weights](#)

Forecasts Error: **NORMAL: 2.16**

[BMA Forecast Verification](#)

[Prob of freezing](#)

[Prob of precip > 0](#)

[Prob of precip > 1/4"](#)

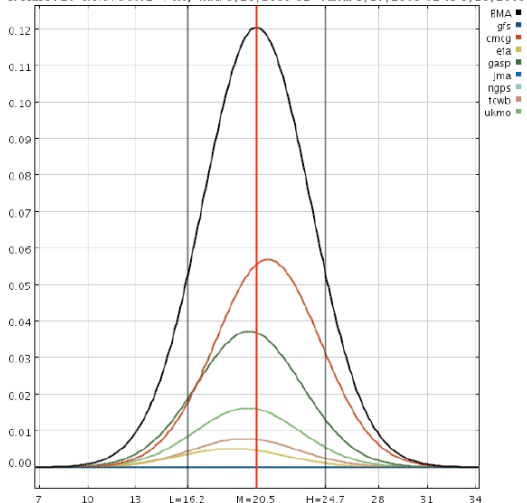
[Prob of precip > 1"](#)

[Prob of high winds](#)

[Prob of gale winds](#)



Forecast PDF 0.0% MAXT2 < 0.0, Init: 5/26/2009 0Z Valid: 5/27/2009 0Z to 5/28/2009



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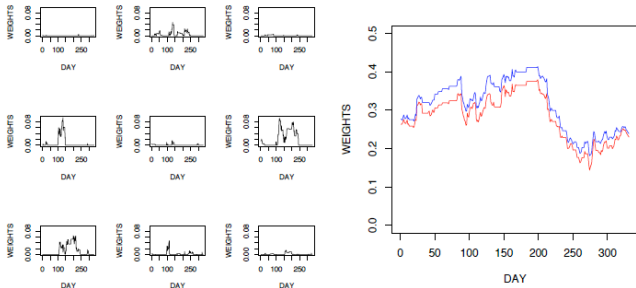
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	MAE		CRPS	
	Raw	BMA	Raw	BMA
UW ME (8)	2.31	2.15	1.96	1.55
UW EnKF (80 exchangeable)	3.32	2.49	2.84	1.76
Combined (89)	3.25	2.09	2.64	1.48

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- Same conclusion with MAE (deterministic) and CRPS (probabilistic)

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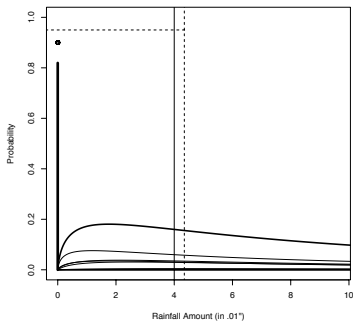
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  - **Zero component not needed in the Pacific Northwest**

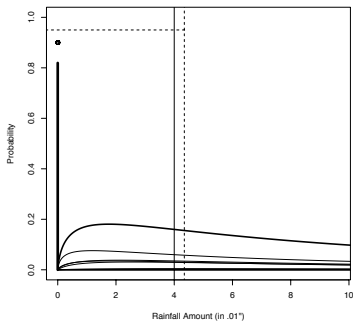
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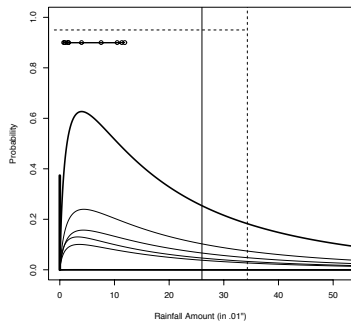


Renton, 19th May, 2003

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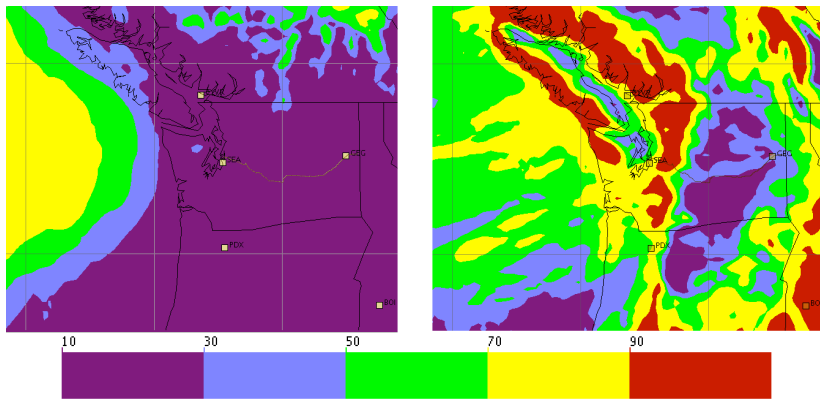


Station KPWT, 26th January, 2003



# BMA Probability of Precipitation

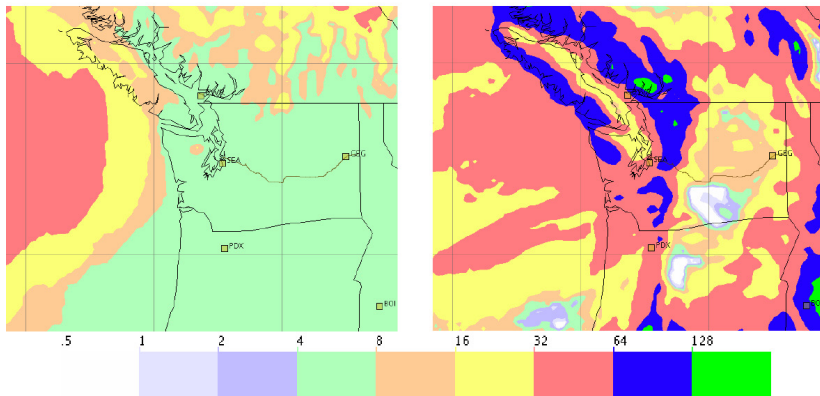
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(a) 19th May, 2003      (b) 26th January, 2003

# BMA 90% Upper Bound forecast

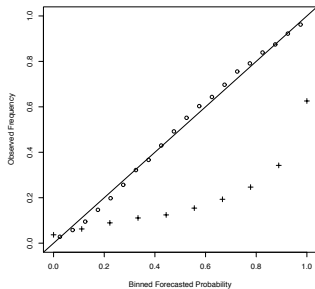
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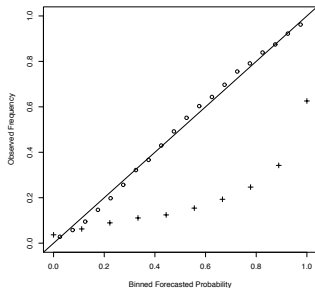
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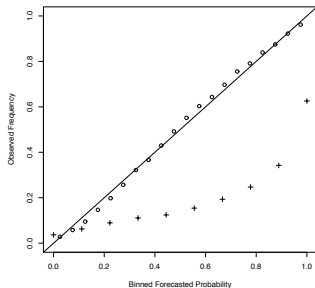


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- x-axis shows the forecast probability of precipitation (PoP)

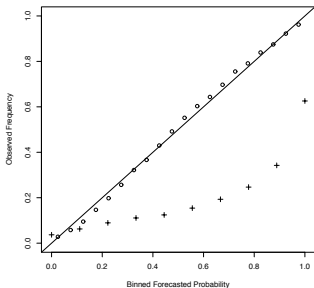
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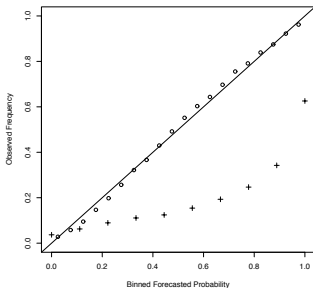


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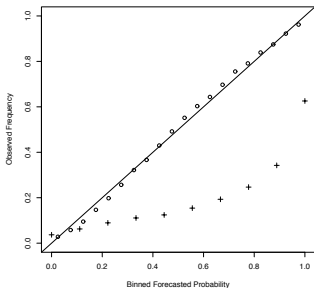
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- Thus a good PoP forecast would be on the diagonal (solid line)

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- y-axis shows the observed relative frequency of precipitation, based on 2 years of data, 2003–2004 (100K obs)
- Thus a good PoP forecast would be on the diagonal (solid line)
- Crosses show the proportion of the ensemble members that predict precipitation, i.e. the raw ensemble PoP forecast. Poorly calibrated

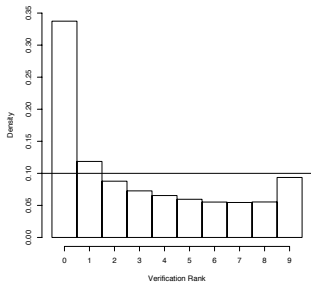
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- Circles show the BMA PoP forecast. Much better.

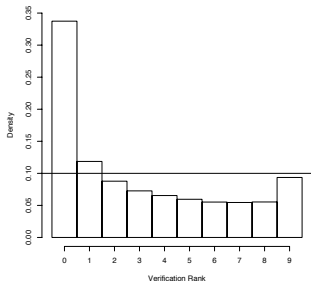
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Verification rank histogram  
for ensemble forecast

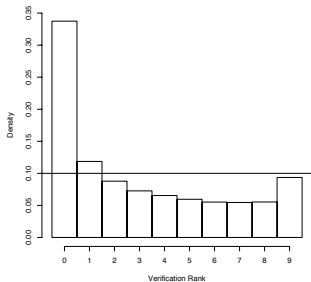
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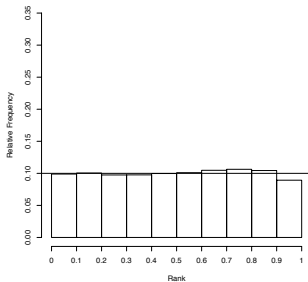
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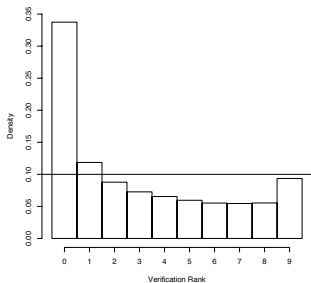
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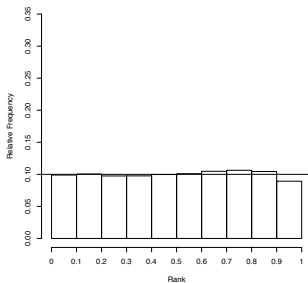
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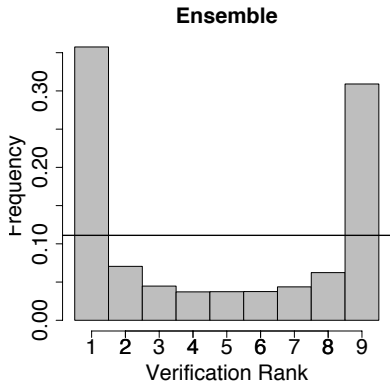


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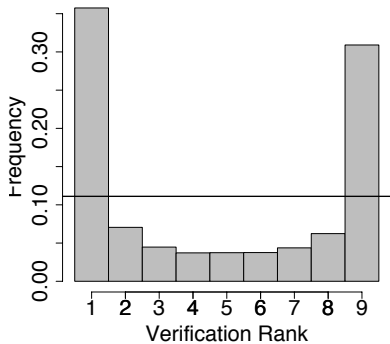
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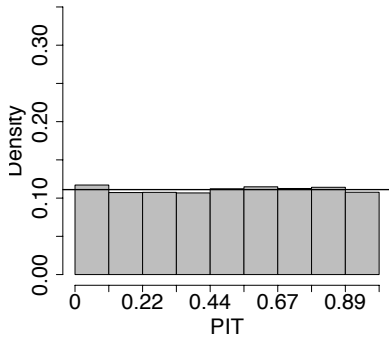
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### Ensemble



### BMA standard



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[www.stat.washington.edu/MURI](http://www.stat.washington.edu/MURI)  
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